## JUNE 1996

## PROVINCIAL EXAMINATION

## MINISTRY OF EDUCATION, SKILLS AND TRAINING

## PHYSICS 12

## GENERAL INSTRUCTIONS

1. Insert the stickers with your Student I.D. Number (PEN) in the allotted spaces above.

Under no circumstance is your name or identification, other than your Student I.D. Number, to appear on this paper.
2. Take the separate Answer Sheet and follow the directions on its front page.
3. Be sure you have an HB pencil and an eraser for completing your Answer Sheet. Follow the directions on the Answer Sheet when answering multiple-choice questions.
4. For each of the written-response questions, write your answer in the space provided.
5. When instructed to open this booklet, check the numbering of the pages to ensure that they are numbered in sequence from page one to the last page, which is identified by

## END OF EXAMINATION.

6. At the end of the examination, place your Answer Sheet inside the front cover of this booklet and return the booklet and your Answer Sheet to the supervisor.

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## PHYSICS 12 JUNE 1996 PROVINCIAL

Course Code $=\mathbf{P H} \quad$ Examination Type $=P$

1. $\quad(7)$
2. 

(7)
3. $\frac{}{(7)}$
4. $\qquad$

Score only one of the following sections.
5. $\qquad$
6.
(7)
7. $\qquad$
Section I
8. $\qquad$
9. $\quad(4)$
or
$\qquad$
10.
11.
(3)
12.
(4)
or
13.
(5)

Section II
(4)
or
15. $\qquad$
16. $\qquad$

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## PHYSICS 12 PROVINCIAL EXAMINATION

## Value <br> Suggested <br> Time

1. This examination consists of three parts:

| PART A: | 30 multiple-choice questions worth <br> two marks each | 60 | 60 |
| :--- | :--- | :--- | :--- |
| PART B: | 7 written-response questions | 48 | 48 |
| PART C: | Elected topics consisting of only <br> written-response questions. <br> Answer only one section. | 12 | 12 |
|  | ( |  |  |

Total: 120 marks
120 minutes
2. The last three pages inside the back cover contain the Data Table, Trigonometric and Other Equations, Equations, and Rough Work for Multiple-Choice. These pages may be detached for convenient reference prior to writing this examination.
3. Rough-work space has been incorporated into the space allowed for answering each written-response question. You may not need all of the space provided to answer each question.
4. An approved scientific calculator is essential for the examination. The calculator must be a hand-held device designed only for mathematical computations such as logarithmic and trigonometric functions. It can be programmable, but must not contain any graphing capabilities. You must not bring into the examination room any devices to support calculators such as manuals, printed or electronic cards, printers, memory expansion chips or cards, or keyboards.
5. You are permitted to use rulers, compasses and protractors.
6. a) Final answers must include appropriate units.
b) Marks will not be deducted for answers expressed to two or three significant figures.
c) In this examination the zero in a number such as 30 shall be considered to be a significant zero.
7. You are expected to communicate your knowledge and understanding of physics principles in a clear and logical manner. Partial marks will be awarded for steps and assumptions leading to a solution. Full marks will not be awarded for providing only a final answer.

If you are unable to determine the value of a quantity required in order to proceed, you may assume a reasonable value and continue toward the solution. Such a solution, however, may not be eligible for full marks.
8. You have two hours to complete this examination.

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Value: 60 marks ( 2 marks per question)
Suggested Time: 60 minutes
INSTRUCTIONS: For each question, select the best answer and record your choice on the Answer Sheet provided. Using an HB pencil, completely fill in the circle that has the letter corresponding to your answer.

1. Which of the following remain(s) constant for a projectile: its horizontal velocity component, $v_{H}$, its vertical velocity component, $v_{V}$, its vertical acceleration, g ?
A. $v_{V}$
B. $g$ and $v_{V}$
C. $\quad g$ and $v_{H}$
D. $g, v_{H}$ and $v_{V}$
2. A pilot points an aircraft due east, while the wind blows from the south.



The resultant velocity of the aircraft over the ground is $64 \mathrm{~m} / \mathrm{s}, 25^{\circ} \mathrm{N}$ of E . At what speed does the wind blow?
A. $2.6 \mathrm{~m} / \mathrm{s}$
B. $27 \mathrm{~m} / \mathrm{s}$
C. $30 \mathrm{~m} / \mathrm{s}$
D. $58 \mathrm{~m} / \mathrm{s}$
3. Gravitational field strength is measured in
A. N
B. $\mathrm{N} / \mathrm{C}$
C. $\mathrm{N} / \mathrm{kg}$
D. $\mathrm{N} \cdot \mathrm{m}^{2} / \mathrm{kg}^{2}$
4. The frictionless system shown below accelerates at $1.60 \mathrm{~m} / \mathrm{s}^{2}$ when released.


Find the tension in the string while the system is accelerating.
A. $\quad 3.20 \mathrm{~N}$
B. $\quad 16.4 \mathrm{~N}$
C. $\quad 19.6 \mathrm{~N}$
D. 22.8 N
5. Force $F$ gives mass $m_{1}$ an acceleration of $4.0 \mathrm{~m} / \mathrm{s}^{2}$. The same force $F$ gives mass $m_{2}$ an acceleration of $2.0 \mathrm{~m} / \mathrm{s}^{2}$. What acceleration would force $F$ give to the two masses $m_{1}$ and $m_{2}$ if they were glued together?
A. $\quad 1.0 \mathrm{~m} / \mathrm{s}^{2}$
B. $\quad 1.3 \mathrm{~m} / \mathrm{s}^{2}$
C. $\quad 3.0 \mathrm{~m} / \mathrm{s}^{2}$
D. $\quad 6.0 \mathrm{~m} / \mathrm{s}^{2}$
6. Are momentum and impulse scalar or vector quantities?
A.

| MOMENTUM | IMPULSE |
| :---: | :---: |
| Scalar | Scalar |
| Scalar | Vector |
| Vector | Scalar |
| Vector | Vector |

7. As a skier descends a slope, her kinetic energy increases from 600 J to 3200 J while her gravitational potential energy decreases by 5900 J . How much heat energy is created due to friction?
A. 2100 J
B. 3300 J
C. 8500 J
D. 9700 J
8. A rock is released from the top of a 30 m-high cliff at the same time as a ball is thrown upwards from the base of the cliff at $20 \mathrm{~m} / \mathrm{s}$. How much time elapses before they collide?
A. 1.0 s
B. $\quad 1.2 \mathrm{~s}$
C. $\quad 1.5 \mathrm{~s}$
D. 2.5 s
9. A 60 kg girl and her 45 kg brother are at rest at the centre of a frozen pond. He pushes her so that she slides away at $2.4 \mathrm{~m} / \mathrm{s}$. How much total work is done? (Ignore friction.)

A. 58 J
B. 170 J
C. 350 J
D. 400 J
10. Two forces, 12 N west and 5.0 N north, act on an object. What is the direction of a third force that would produce static equilibrium?
A. $23^{\circ}$ south of east
B. $23^{\circ}$ north of west
C. $67^{\circ}$ south of east
D. $67^{\circ}$ north of west
11. A 3.0 m uniform beam of mass 15 kg is pivoted 1.0 m from the end as shown below.


A 35 kg child sits 0.60 m from the pivot. How far, $\boldsymbol{d}$, from the pivot, must a 20 kg child sit in order for the beam to be in equilibrium?
A. 0.68 m
B. 1.0 m
C. $\quad 1.1 \mathrm{~m}$
D. 1.4 m
12. The diagram below shows the path of a planet orbiting a central mass.

Area 1


The two areas are swept out in equal intervals of time. How does Area 1 compare to Area 2?
A. Area 1 is equal to Area 2.
B. Area 1 is less than Area 2.
C. Area 1 is greater than Area 2.
D. Insufficient information is given to compare the two areas.
13. An object of mass $\boldsymbol{m}$ is on a horizontal rotating platform. The mass is located 0.22 m from the axle and makes one revolution every 0.74 s .


The friction force needed to keep the mass from sliding is 13 N . What is the object's mass?
A. 0.82 kg
B. $\quad 1.3 \mathrm{~kg}$
C. 2.7 kg
D. 5.2 kg
14. A 1500 kg spaceship circles a planet once every $4.0 \times 10^{5} \mathrm{~s}$ with an orbital radius of $3.6 \times 10^{7} \mathrm{~m}$. What is the mass of this planet?
A. $\quad 2.0 \times 10^{11} \mathrm{~kg}$
B. $\quad 1.2 \times 10^{12} \mathrm{~kg}$
C. $\quad 1.7 \times 10^{23} \mathrm{~kg}$
D. $2.6 \times 10^{26} \mathrm{~kg}$
15. An object is located on the surface of a planet. The work required to remove this object from the planet's gravitational field depends on which combination of the following three variables: mass of the planet, mass of the object, and radius of the planet?
A.

| MASS OF PLANET | MASS OF OBJECT | RADIUS OF PLANET |
| :---: | :---: | :---: |
| Yes | Yes | Yes |
| Yes | Yes | No |
| Yes | No | Yes |
| No | Yes | Yes |

16. Which of the following diagrams best shows the electric field between two equal negative charges?
A.

B.

C.

D.

17. In a hydrogen atom, the electron and proton are separated by a distance of $5.3 \times 10^{-11} \mathrm{~m}$. What is the electric force exerted on the proton by the electron?
A. 0 N
B. $\quad 4.4 \times 10^{-18} \mathrm{~N}$
C. $8.2 \times 10^{-8} \mathrm{~N}$
D. $1.0 \times 10^{12} \mathrm{~N}$
18. A 2.5 C charge is moved from a point with a potential of 12 V to another point of potential 75 V . How much work was done on this charge?
A. 30 J
B. 160 J
C. 180 J
D. 220 J
19. An object with a charge of $+4.0 \times 10^{-18} \mathrm{C}$ and a mass of $1.1 \times 10^{-15} \mathrm{~kg}$ is held stationary by balanced gravitational and electric forces midway between horizontal charged plates as shown. What is the applied voltage $V$ ?

A. 16 V
B. 32 V
C. 65 V
D. $2.7 \times 10^{2} \mathrm{~V}$
20. Which of the following instruments will measure the emf of a cell without drawing any current?
A. ammeter
B. voltmeter
C. ohmmeter
D. potentiometer
21. Which of the following arrangements would draw the largest current when connected to a potential difference? All resistors have the same value.
A.

B.

C.

D.

22. In the following circuit, what current flows through the $4.0 \Omega$ resistor?

A. 2.4 A
B. 2.6 A
C. 3.0 A
D. 4.0 A
23. In the following circuit, what is the magnitude of the potential difference between $\mathbf{X}$ and $\mathbf{Y}$ ?

A. 3.0 V
B. $\quad 6.0 \mathrm{~V}$
C. 9.0 V
D. 12 V
24. Which of the following diagrams best represents the magnetic field in the region between north and south poles of a pair of permanent magnets?
A.

B.

C.

D.

25. A long conductor is placed in a 0.20 T magnetic field as shown in the diagram below.


What are the magnitude and direction of the magnetic force on the conductor when it carries a current of 12 A ?

|  | MAGNITUDE OF THE <br> MAGNETIC FORCE | DIRECTION OF THE <br> MAGNETIC FORCE |
| :--- | :---: | :---: |
| A. | 0.36 N | Up the page |
| B. | 0.36 N | Down the page |
| C. | 0.96 N | Up the page |
| D. | 0.96 N | Down the page |
|  |  |  |

26. A 150 turn coil has an area of $2.4 \times 10^{-4} \mathrm{~m}^{2}$. What magnetic field strength will produce a maximum torque of $2.2 \times 10^{-3} \mathrm{~N} \cdot \mathrm{~m}$ on the coil when a 0.20 A current flows through it?
A. $1.6 \times 10^{-5} \mathrm{~T}$
B. 0.13 T
C. 0.31 T
D. 3.3 T
27. A conductor is initially at rest in a magnetic field.


In which direction should the conductor be moved so that the end nearest $\mathbf{X}$ becomes positive?
A. 1
B. 2
C. 3
D. 4
28. A coil of 150 turns and an area of $2.0 \times 10^{-4} \mathrm{~m}^{2}$ is placed in a 1.00 T magnetic field as shown in Diagram I.


Diagram I


Diagram II

If this field changes to 0.45 T in 0.060 s , what is the average emf induced in the coil and in what direction does the induced current flow?
A.

| InDUCED EMF $(V)$ | CURRENT DIRECTION |
| :---: | :---: |
| 0.28 | Clockwise |
| 0.28 | Counterclockwise |
| 0.36 | Clockwise |
| 0.36 | Counterclockwise |

29. A dc motor has an armature resistance of $3.0 \Omega$. When connected to a 24 V source the motor draws 1.4 A at maximum speed. What is the back emf produced by the motor at maximum speed?
A. 4.2 V
B. 20 V
C. 24 V
D. 28 V
30. A soldering iron transformer has 200 primary turns and 5 secondary turns. The primary draws 0.80 A at 120 V . Which of the following gives the secondary current and secondary voltage?

|  | SECONDARY CURRENT | SECONDARY VOLTAGE |
| :--- | :---: | :---: |
| A. | 0.020 A | 4800 V |
| B. | 0.80 A | 120 V |
| C. | 4.0 A | 24 V |
| D. | 32 A | 3.0 V |
|  |  |  |

This is the end of the multiple-choice section.
Answer the remaining questions directly in this examination booklet.

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Value: 48 marks
Suggested Time: 48 minutes
INSTRUCTIONS:

1. Rough-work space has been incorporated into the space allowed for answering each written-response question. You may not need all of the space provided to answer each question.
2. a) Final answers must include appropriate units.
b) Marks will not be deducted for answers expressed to two or three significant figures.
c) In this examination the zero in a number such as 30 shall be considered to be a significant zero.
3. You are expected to communicate your knowledge and understanding of physics principles in a clear and logical manner. If you are unable to determine the value of a quantity required in order to proceed, you may assume a reasonable value and continue toward the solution. Partial marks will be awarded for steps and assumptions leading to a solution. Such a solution, however, may not be eligible for full marks.

Full marks will NOT be given for the final answer only.

1. A soccer ball is kicked over level ground with an initial velocity of $18 \mathrm{~m} / \mathrm{s}, 24^{\circ}$ above the horizontal.
a) How long does it take the ball to return to the ground?
(4 marks)
b) What is the range of the ball?

| ANSWER: |
| :--- | :--- |
| a) time:_-_ $\quad$Score for <br> b) range: <br> Question 1: |
| $1 . \overline{(7)}$ |

OVER
2. Two air pucks approach each other, stick together and then travel due east as shown below. Find the initial velocity (magnitude and direction) of puck $\mathbf{A}$.

Before collision


After collision


| ANSWER: | Score for <br> Question 2: |
| :--- | :--- |
| magnitude: |  |
| direction: | $2 . \overline{(7)}$ |

3. A uniform 350 kg beam of length 4.2 m is held stationary by a horizontal cable. The cable is attached to a point on the beam 3.0 m from the hinge.

a) Draw and label a free body diagram showing the forces on the beam.
b) If the maximum tension the cable can withstand is $1.3 \times 10^{4} \mathrm{~N}$, what maximum mass, $\boldsymbol{m}$, can be suspended from the end of the beam?
(5 marks)

| ANSWER: | Score for <br> Question 3: |
| :--- | :--- |
| b) mass:_- | $3 . \overline{(7)}$ |

4. A 35 kg child rides a ferris wheel of radius 12 m . The child moves in a vertical circle at a constant speed and completes one rotation every 9.0 s .

a) As the child travels over the top, what is the magnitude of the force that the seat exerts on the child?
b) How does the magnitude of the child's acceleration at the top of the ride compare to her acceleration at the bottom?

The child's acceleration at the top is: (circle one)
(1 mark)
i) less than at the bottom.
ii) greater than at the bottom.
iii) the same as at the bottom.

Explain your choice using principles of physics.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

ANSWER:
Score for Question 4:
4.
5. A proton is located at $\mathbf{A}, 1.0 \mathrm{~m}$ from a fixed $+2.2 \times 10^{-6} \mathrm{C}$ charge.

a) What is the change in potential energy of the proton as it moves to $\mathbf{B}, 10 \mathrm{~m}$ from the fixed charge?

| ANSWER: | Score for <br> Question 5: |
| :--- | :--- |
| a) change in potential energy:___ <br> b) speed: | $5 . \overline{(7)}$ |

6. A beam of electrons travelling at $1.8 \times 10^{8} \mathrm{~m} / \mathrm{s}$ is directed towards a 0.014 T magnetic field as shown in the diagram below.

a) Which of the following diagrams illustrates the path of the electron beam once in the magnetic field? (Circle one.)


| ANSWER: | Score for <br> Question 6: |
| :--- | :--- |
| b) radius:__ | $6 . \overline{(7)}$ |

7. Electrical power is transmitted over large distances at very high voltages. Using principles of physics, explain how high voltages reduce power losses in transmission lines.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

PART C: ELECTED TOPICS

Value: 12 marks
Suggested Time: 12 minutes

## INSTRUCTIONS

1. Choose only one section from the three sections in this part of the examination.

SECTION I: Quantum Mechanics (p. 28 to 31)
or
SECTION II: Fluid Theory (p. 32 to 35)
or
SECTION III: AC Circuitry and Electronics (p. 36 to 39)
2. If you answer questions in more than one section, only the answers in the first section chosen will be marked.
3. Answer all of the questions in the section that you choose. Write your answers in the space provided in this booklet.
4. Rough-work space has been incorporated into the space allowed for answering each question. You may not need all of the space provided to answer each question.
5. a) Final answers must include appropriate units.
b) Marks will not be deducted for answers expressed to two or three significant figures.
c) In this examination the zero in a number such as 30 shall be considered to be a significant zero.
6. Since partial marks will be awarded for a partial solution, it is important that you provide a clear indication of the steps leading to your answer.

Full marks will NOT be given for the final answer only.

I have selected SECTION $\qquad$ .

## SECTION I: Quantum Mechanics

1. What is the energy of a photon of light of wavelength 550 nm ?
(3 marks)

| ANSWER: | Score for <br> Question 1: |
| :--- | :--- |
| energy:-_ | $8 . \overline{(3)}$ |

## SECTION I: Continued

2. The work function for a metal is 1.65 eV . If the incident light has a wavelength of 410 nm , what would be the maximum speed of the emitted photoelectrons at the metal's surface?

| ANSWER: | Score for <br> Question 2: |
| :--- | :--- |
| maximum speed: | $9 . \overline{(4)}$ |

## SECTION I: Continued

3. What is the momentum of the photon emitted when the electron in a hydrogen atom changes from the $n=4$ to $n=1$ state? (5 marks)

| ANSWER: | Score for <br> Question 3: |
| :--- | :--- |
| momentum of photon:_ـ_ | $10 . \overline{(5)}$ |

## END OF SECTION I: Quantum Mechanics

## SECTION II: Fluid Theory

1. A solid uniform cube of unknown material is 0.13 m on a side and has a mass of 2.0 kg . What is the density of this cube?

| ANSWER: | Score for <br> Question 1: |
| :--- | :--- |
| density: - | $11 . \overline{(3)}$ |

## SECTION II: Continued

2. A rigid sealed container is filled with a gas. Initially the gas is at a temperature of $28^{\circ} \mathrm{C}$ and at a pressure of $4.0 \times 10^{5} \mathrm{~Pa}$. If the gas is then heated to a temperature of $52^{\circ} \mathrm{C}$, what is the new pressure in the container?
(4 marks)

| ANSWER: | Score for <br> Question 2: |
| :--- | :---: |
| pressure:__ | $12 . \overline{(4)}$ |

## SECTION II: Continued

3. The pressure of the compressed air inside the tank shown below is $1.5 \times 10^{4} \mathrm{~Pa}$ greater than the outside air pressure. There is a small hole in the side of the tank, 4.2 m below water level.


What is the speed of the water leaving this hole?
(5 marks)

| ANSWER: | Score for <br> Question 3: |
| :--- | :--- |
| speed:_- | $13 . \overline{(5)}$ |

## END OF SECTION II: Fluid Theory

## SECTION III: AC Circuitry and Electronics

1. What is the total capacitance between points $\mathbf{A}$ and $\mathbf{B}$ in the diagram below?


| ANSWER: | Score for <br> Question 1: |
| :--- | :--- |
| total capacitance: $\quad 14 . \overline{(3)}$ |  |

## SECTION III: Continued

2. a) What is the time constant for the circuit shown below?

b) What is the voltage across the capacitor when the battery has been connected for one time constant?

| ANSWER: | Score for <br> Question 2: |
| :--- | :--- |
| a) time constant:___ | $15 . \overline{(4)}$ |

## SECTION III: Continued

3. What is the impedance of the LCR circuit shown below?


| ANSWER: | Score for <br> Question 3: |
| :--- | :--- |
| impedance: —— | $16 . \overline{(5)}$ |

END OF SECTION III: AC Circuitry and Electronics

## END OF EXAMINATION

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Gravitational constant $\mathrm{G}=6.67 \times 10^{-11} \mathrm{~N} \cdot \mathrm{~m}^{2} / \mathrm{kg}^{2}$

Acceleration due to gravity at the surface of Earth (for the purposes of this examination) $\mathrm{g}=9.80 \mathrm{~m} / \mathrm{s}^{2}$

Earth

| radius | $=6.38 \times 10^{6} \mathrm{~m}$ |
| :---: | :---: |
| radius of orbit about Sun | $=1.50 \times 10^{11} \mathrm{~m}$ |
| period of rotation | $=8.61 \times 10^{4} \mathrm{~s}$ |
| period of revolution about Sun. | $=3.16 \times 10^{7} \mathrm{~s}$ |
| ma | $=5.98 \times 10^{24} \mathrm{~kg}$ |

## Moon

> radius
> $=1.74 \times 10^{6} \mathrm{~m}$
> radius of orbit about Earth
> $=3.84 \times 10^{8} \mathrm{~m}$
> period of rotation
> $=2.36 \times 10^{6} \mathrm{~s}$
> period of revolution about Earth
> $=2.36 \times 10^{6} \mathrm{~s}$
> mass
> $=7.35 \times 10^{22} \mathrm{~kg}$

Sun
mass
$=1.98 \times 10^{30} \mathrm{~kg}$
Constant in Coulomb's Law
$\mathrm{k}=9.00 \times 10^{9} \mathrm{~N} \cdot \mathrm{~m}^{2} / \mathrm{C}^{2}$
Elementary charge
$\mathrm{e}=1.60 \times 10^{-19} \mathrm{C}$
Mass of electron
$\mathrm{m}_{\mathrm{e}}=9.11 \times 10^{-31} \mathrm{~kg}$
Mass of proton
$m_{p}=1.67 \times 10^{-27} \mathrm{~kg}$
Mass of neutron
$\mathrm{m}_{\mathrm{n}}=1.68 \times 10^{-27} \mathrm{~kg}$
Permeability of free space
$\mu_{\mathrm{o}}=4 \pi \times 10^{-7} \mathrm{~T} \cdot \mathrm{~m} / \mathrm{A}$
Planck's constant
$\mathrm{h}=6.63 \times 10^{-34} \mathrm{~J} \cdot \mathrm{~s}$
$\mathrm{h}=4.14 \times 10^{-15} \mathrm{eV} \cdot \mathrm{s}$
Speed of light
c $=3.00 \times 10^{8} \mathrm{~m} / \mathrm{s}$
Rydberg's constant
$\mathrm{R}=1.097 \times 10^{7} \mathrm{~m}^{-1}$
Unified atomic mass unit
$\mathrm{u}=1.66 \times 10^{-27} \mathrm{~kg}$
Boltzmann's constant
$\mathrm{k}=1.38 \times 10^{-23} \mathrm{~J} / \mathrm{K}$
Gas constant
$\mathrm{R}=8.31 \mathrm{~J} / \mathrm{mol} \cdot \mathrm{K}$
Density of water
$=1.00 \times 10^{3} \mathrm{~kg} / \mathrm{m}^{3}$
Density of air
$=1.29 \mathrm{~kg} / \mathrm{m}^{3}$
Standard atmospheric pressure
$=1.01 \times 10^{5} \mathrm{~Pa}$
Volume of one mole of gas at STP
$=22.4 \mathrm{~L}\left(2.24 \times 10^{-2} \mathrm{~m}^{3}\right)$
Avogadro's number
Absolute zero
$\mathrm{N}=6.02 \times 10^{23}$ particles $/ \mathrm{mol}$
$=-273^{\circ} \mathrm{C}$

## For Right-angled Triangles:



$$
\begin{aligned}
& a^{2}+b^{2}=c^{2} \\
& \sin \theta=\frac{b}{c} \quad \cos \theta=\frac{a}{c} \quad \tan \theta=\frac{b}{a}
\end{aligned}
$$

$$
\text { area }=\frac{1}{2} a b
$$

## For All Triangles:



$$
\begin{aligned}
& \text { area }=\frac{1}{2} \text { base } \times \text { height } \\
& \sin 2 \mathrm{~A}=2 \sin \mathrm{~A} \cos \mathrm{~A}
\end{aligned}
$$

Sine Law: $\quad \frac{\sin \mathrm{A}}{a}=\frac{\sin \mathrm{B}}{b}=\frac{\sin \mathrm{C}}{c}$

Cosine Law: $c^{2}=a^{2}+b^{2}-2 a b \cos \mathrm{C}$

## Circle:

Circumference $=2 \pi r$

$$
\text { Area }=\pi r^{2}
$$

## Sphere:

Surface area $=4 \pi r^{2}$

Volume $=\frac{4}{3} \pi r^{3}$

## Quadratic Equation:

If $a x^{2}+b x+c=0$, then $x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$

Note: Vector quantities have not been indicated.

1. Kinematics: (for constant acceleration)
$v=v_{0}+a t$

$$
v_{a v}=\frac{v+v_{0}}{2}
$$

$$
v^{2}=v_{0}^{2}+2 a d
$$

$$
d=v_{0} t+\frac{1}{2} a t^{2}
$$

2. Dynamics:

$$
F_{\mathrm{f}}=\mu F_{\mathrm{N}} \quad F_{\text {net }}=m a
$$

3. Mechanical Energy and Momentum:
$W=F d$
$E_{\mathrm{p}}=m g h$
$E_{\mathrm{k}}=\frac{1}{2} m v^{2}$
$P=\frac{W}{t}$
$p=m v$
$\Delta p=F_{\text {net }} \Delta t$
4. Equilibrium:

$$
\tau=F d
$$

5. Circular Motion and Gravitation:

$$
\begin{array}{ll}
a_{\mathrm{c}}=\frac{v^{2}}{r}=\frac{4 \pi^{2} r}{T^{2}} & F=G \frac{m_{1} m_{2}}{r^{2}} \\
E_{\mathrm{p}}=-G \frac{m_{1} m_{2}}{r} & r^{3} \propto T^{2}
\end{array}
$$

6. Electrostatics:
$F=k \frac{Q_{1} Q_{2}}{r^{2}}$
$E=\frac{V}{d}$
$V=\frac{k Q}{r}$
$E_{\mathrm{p}}=k \frac{Q_{1} Q_{2}}{r}$
$F=Q E$
$V=\frac{\Delta E_{\mathrm{p}}}{Q}$

## 7. Circuitry:

$$
Q=I t
$$

$$
V=I R
$$

$$
P=V I
$$

## 8. Electromagnetism:

$F=I l B$

$$
B=\frac{\mu_{0} I}{2 \pi d}
$$

$$
\tau=N I A B
$$

$$
F=Q v B
$$

$$
B=\mu_{0} n I\left(\text { where } n=\frac{N}{l}\right)
$$

$$
\Phi=B A
$$

$$
\varepsilon=-N \frac{\Delta \Phi}{\Delta t}
$$

$$
\varepsilon=B l v
$$

$$
\frac{V_{\mathrm{s}}}{V_{\mathrm{p}}}=\frac{N_{\mathrm{s}}}{N_{\mathrm{p}}}
$$

9. Quantum Mechanics: (Section I)

$$
\begin{array}{lll}
E=h f & c=f \lambda & E_{\mathrm{n}}=(-13.6 \mathrm{eV}) \frac{Z^{2}}{n^{2}} \\
E_{\mathrm{k}_{\max }}=h f-W_{0} & \lambda=\frac{h}{p} &
\end{array}
$$

10. Fluid Theory: (Section II)
$\rho=\frac{m}{V}$
$P V=N k T$
$P V=\frac{1}{3} N m v^{2}$
$F=\rho V g$
$P=\frac{F}{A}$
$P=P_{\mathrm{G}}+P_{\mathrm{a}}$
$P V=n R T$
$P+\frac{1}{2} \rho v^{2}+\rho g h=$ constant
$E_{\mathrm{k}}=\frac{3}{2} k T$
11. AC Circuits and Electronics: (Section III)

$$
\begin{array}{lll}
Q=C V & E_{p}=\frac{1}{2} C V^{2} & \tau=R C \\
X_{\mathrm{C}}=\frac{1}{2 \pi f C} & Z=\sqrt{R^{2}+\left(X_{\mathrm{L}}-X_{\mathrm{C}}\right)^{2}} & X_{\mathrm{L}}=2 \pi f L \\
f_{0}=\frac{1}{2 \pi \sqrt{L C}} & \beta \text { (current gain })=\frac{\Delta I_{C}}{\Delta I_{B}} & A_{\mathrm{f}}=\frac{A}{1-\beta A}
\end{array}
$$

(where $\beta=$ feedback ratio)

You may detach this page for convenient reference. Exercise care when tearing along perforations.

