## Physics 12

August 2000 Provincial Examination

## Answer Key / Scoring Guide

## CURRICULUM:

## Organizers

1. Vector Kinematics in Two Dimensions and Dynamics and Vector Dynamics
2. Work, Energy and Power
and
Momentum
3. Equilibrium
4. Circular Motion
and
Gravitation
5. Electrostatics
6. Electric Circuits
7. Electromagnetism

Sub-Organizers
A, B

C, D
E
F, G
H
I

J
K, L
$\mathrm{M}, \mathrm{N}$
O, P

PART A: Multiple Choice (each question worth TWO marks)

| Q | K | C | CO | PLO | Q | K | C | CO | PLO |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1. | D | K | 1 | C2, 3 | 16. | D | U | 4 | J2 |
| 2. | B | U | 1 | C4, 3 | 17. | A | U | 4 | J6 |
| 3. | C | U | 1 | C4 | 18. | D | K | 4 | K7 |
| 4. | A | U | 1 | C8, D5 | 19. | B | U | 5 | K5 |
| 5. | A | U | 1 | D6 | 20. | B | H | 5 | L6 |
| 6. | A | K | 2 | E8 | 21. | A | K | 5 | M4, A10 |
| 7. | B | U | 2 | E10 | 22. | B | U | 6 | M11, 6 |
| 8. | C | U | 2 | E7 | 23. | C | H | 6 | M6, 7 |
| 9. | B | H | 2 | E7, B8 | 24. | C | K | 6 | O2 |
| 10. | D | K | 3 | H4 | 25. | B | U | 7 | O4 |
| 11. | B | U | 3 | H3 | 26. | A | U | 7 | O6 |
| 12. | A | K | 3 | I1, 2 | 27. | B | U | 7 | O7 |
| 13. | C | U | 4 | I4 | 28. | B | U | 7 | P5, 3 |
| 14. | D | U | 4 | I4 | 29. | B | U | 7 | P8, 9 |
| 15. | D | K | 4 | J4 | 30. | A | U | 7 | P11 |

Multiple Choice $=\mathbf{6 0}$ marks

## PART B: Written Response

| Q | B | C | S | CO | PLO |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1. | 1 | U | 7 | 1 | A9 |
| 2. | 2 | U | 9 | 2 | F4, 7 |
| 3. | 3 | U | 7 | 3 | H11 |
| 4. | 4 | U | 7 | 4 | J7 |
| 5. | 5 | U | 7 | 5 | L6 |
| 6. | 6 | U | 7 | 6 | M5, 6, 7, N2 |
| 7. | 7 | U | 7 | 7 | O8, P3 |
| 8 | 8 | H | 5 | 1, 2 | A10, E10 |
| 9. | 9 | H | 4 | 3 | H2, H3 |

Multiple Choice $=60$ (30 questions)
Written Response $=60$ ( 9 questions)
EXAMINATION TOTAL = $\mathbf{1 2 0}$ marks
LEGEND:
Q = Question Number
B = Score Box Number
C = Cognitive Level
$\mathbf{C O}=$ Curriculum Organizer
$\mathbf{K}=$ Keyed Response
$\mathbf{S}=$ Score
PLO = Prescribed Learning Outcome

1. An aircraft heads due south with a speed relative to the air of $44 \mathrm{~m} / \mathrm{s}$. Its resultant speed over the ground is $47 \mathrm{~m} / \mathrm{s}$. The wind blows from the west.
a) What is the speed of the wind?

$$
\begin{aligned}
& \vec{v}_{P A}=44 \mathrm{~m} / \mathrm{s} \\
& v_{P A}^{2}+v_{A G}^{2}={\stackrel{v}{v_{P G}}}_{2}^{\alpha}=47 \mathrm{~m} / \mathrm{s} \quad \leftarrow \mathbf{2} \text { marks for diagram } \\
& 44^{2}+v_{A G}^{2}=47^{2} \\
& v_{A G}=16.5 \mathrm{~m} / \mathrm{s} \\
& v_{A G}=17 \mathrm{~m} / \mathrm{s} \quad \leftarrow \mathbf{1} \text { mark }
\end{aligned}
$$

b) What is the direction of the aircraft's path over the ground?

$$
\begin{aligned}
\cos \alpha & =\frac{44}{47} \quad \leftarrow \mathbf{1} \frac{1}{2} \text { marks } \\
\alpha & =20.6^{\circ} \\
& =\underbrace{21^{\circ}}_{\mathbf{1} \text { mark }} \underbrace{\text { east of south }}_{\frac{\mathbf{1}}{\mathbf{2}} \text { mark }}
\end{aligned}
$$

or
$69^{\circ}$ south of east
or
south $21^{\circ}$ east
2. A space vehicle made up of two parts is travelling at $230 \mathrm{~m} / \mathrm{s}$ as shown.


An explosion causes the 450 kg part to separate and travel with a final velocity of $280 \mathrm{~m} / \mathrm{s}$ as shown.

a) What was the momentum of the space vehicle before the explosion?

$$
\begin{aligned}
\rho & =m v \\
& =(1200+450) 230 \\
& =3.8 \times 10^{5} \mathrm{~kg} \mathrm{~m} / \mathrm{s} \quad \leftarrow \mathbf{2} \text { marks }
\end{aligned}
$$

b) What was the magnitude of the impulse on the 1200 kg part during the separation?

$$
\begin{aligned}
\text { Impulse } & =\Delta p \\
& =P_{b}-P_{a} \\
& =(450 \times 280)-(450 \times 230) \\
& =2.3 \times 10^{4} \mathrm{~N} \cdot \mathrm{~s}
\end{aligned}
$$

$\leftarrow 1$ mark
$\leftarrow 1$ mark
$\leftarrow \mathbf{1}$ mark
c) Using principles of physics, explain what changes occur, if any, to the i) momentum of the system as a result of the explosion.

In an explosion, momentum must be conserved.
ii) kinetic energy of the system as a result of the explosion.

Since the explosion adds energy to the system, the system will gain kinetic energy.
3. A uniform 1200 kg steel girder is supported horizontally at its endpoints as shown in the diagram.


What are the upward forces at the girder end points when it is bearing a 3700 kg shipping container 8.0 m from support A?


## Pivot A (4 marks for first pivot calculation):

$$
\left.\begin{array}{rl}
\Sigma \tau_{c w} & =\Sigma \tau_{c c w} \\
F_{C} L_{C}+F_{W} L_{W} & =F_{B} L_{B} \\
3700(9.8)(8)+1200(9.8)(16) & =F_{B}(32)
\end{array}\right\} \leftarrow \mathbf{1} \text { mark } ~ \leftarrow \mathbf{2} \text { marks }
$$

Pivot B (3 marks for second pivot OR sum of forces):
$\left.\begin{array}{rl}F_{C} L_{C}+F_{W} L_{W}=F_{A} L_{A} \\ 3700(9.8)(24)+1200(9.8)(16)= & F_{A}(32) \\ \left(8.70 \times 10^{5}\right)+\left(1.88 \times 10^{5}\right) & =F_{A}(32)\end{array}\right\} \leftarrow \mathbf{2}$ marks

## Forces:

$$
\left.\begin{array}{rl}
F_{C}+F_{W}=F_{A}+F_{B} \\
3700(9.8)+1200(9.8)=F_{A}+F_{B} \\
\left(3.63 \times 10^{4}\right)+\left(1.18 \times 10^{4}\right)=F_{A}+F_{B}
\end{array}\right\} \leftarrow \mathbf{2} \text { marks } \quad \begin{aligned}
F_{A} \text { or } F_{B}= & \leftarrow \mathbf{1} \text { mark }
\end{aligned}
$$

4. A $4.00 \times 10^{3} \mathrm{~kg}$ object is lifted from the earth's surface to an altitude of $3.2 \times 10^{5} \mathrm{~m}$. How much work does this require?

(Diagram not to scale.)
$R_{1}=6.38 \times 10^{6} \mathrm{~m}$
$R_{2}=6.38 \times 10^{6} \mathrm{~m}+3.2 \times 10^{5} \mathrm{~m}$

$$
=6.70 \times 10^{6} \mathrm{~m}
$$

$\leftarrow 1$ mark
$W=\Delta E$
$\leftarrow \mathbf{1}$ mark
$\Delta E p=E p_{2}-E p_{1}$

$$
=\frac{-G M m}{R_{2}}-\left(-\frac{G M m}{R_{1}}\right)
$$

$\leftarrow 1$ mark
$=\frac{-6.67 \times 10^{-11} \cdot 5.98 \times 10^{24} \cdot 4.00 \times 10^{3}}{6.70 \times 10^{6}}-\frac{-6.67 \times 10^{-11} \cdot 5.98 \times 10^{24} \cdot 4.00 \times 10^{3}}{6.38 \times 10^{6}}$ $=-2.38 \times 10^{11} \mathrm{~J}-\left(-2.50 \times 10^{11} \mathrm{~J}\right)$
$\leftarrow \mathbf{2}$ marks
$\leftarrow \mathbf{1}$ mark
$\Delta E p=1.2 \times 10^{10} \mathrm{~J}$
$\leftarrow 1$ mark
5. A proton, initially at rest at point $X$, will have what speed at point $Y$ ?
(7 marks)


$$
\begin{aligned}
& \Delta E=0 \\
& \left.\Delta E_{k}=-\Delta E p \quad\right\} \leftarrow \mathbf{1} \text { mark } \\
& E_{k_{2}}-E_{k_{1}}=E_{p_{1}}-E_{p_{2}} \\
& \frac{1}{2} m v_{2}^{2}-0=\frac{k Q q}{r_{1}}-\frac{k Q q}{r_{2}} \quad \leftarrow \mathbf{3} \text { marks } \\
& =\frac{9.0 \times 10^{9} \cdot 3.5 \times 10^{-6} \cdot 1.6 \times 10^{-19}}{1.0}-\frac{9.0 \times 10^{9} \cdot 3.5 \times 10^{-6} \cdot 1.6 \times 10^{-19}}{3.0} \leftarrow \mathbf{2} \text { marks } \\
& =\frac{5.04 \times 10^{-15}}{1}-\frac{5.04 \times 10^{-15}}{3} \\
& =5.04 \times 10^{-15}-1.68 \times 10^{-15} \\
& \frac{1}{2} m v^{2}=3.36 \times 10^{-15} \\
& \frac{1}{2}\left(1.67 \times 10^{-27}\right) v^{2}=3.36 \times 10^{-15} \\
& v=2.0 \times 10^{6} \mathrm{~m} / \mathrm{s} \quad \leftarrow \mathbf{1} \text { mark }
\end{aligned}
$$

6. What is the power dissipated in the $8.0 \Omega$ resistor in the circuit as shown?


$$
\begin{aligned}
\frac{1}{R_{\| \|}} & =\frac{1}{R_{3}}+\frac{1}{R_{4}} \\
& =\frac{1}{12.0}+\frac{1}{8.0} \\
R_{\|} & =4.8 \Omega \quad \leftarrow \mathbf{1} \text { mark } \\
R_{t} & =R_{1}+R_{2}+R_{\|} \\
& =(12.0+10.0+4.8) \\
R_{t} & =26.8 \Omega \\
I_{t} & =\frac{V_{t}}{R_{t}}=\frac{80.0}{26.8}=2.99 \mathrm{~A} \quad \leftarrow \mathbf{2} \text { marks } \\
V_{1} & =I_{t} R_{1}=2.99(12)=35.9 \mathrm{~V} \\
V_{2} & =I \cdot R_{2}=2.99(10)=29.9 \mathrm{~V} \\
V_{\| \|} & =80.0-(35.9+29.9) \\
& =14.3 \mathrm{~V} \\
P & =\frac{V^{2}}{R}=\frac{14.3^{2}}{8.0}=26 \mathrm{~W}
\end{aligned}
$$

7. The magnetic field at the centre of a solenoid of length 0.25 m is $1.2 \times 10^{-2} \mathrm{~T}$. The current in the windings is 7.5 A .
a) How many windings does the solenoid have?

$$
\begin{array}{rlrl}
B & =\mu_{0}\left(\frac{N}{\ell}\right) I & \leftarrow \mathbf{1} \text { mark } \\
N & =\frac{B \ell}{\mu_{0} \cdot I} & \\
& =\frac{\left(1.2 \times 10^{-2}\right)(0.25)}{\left(4 \pi \times 10^{-7}\right)(7 \cdot 5)} & \} \leftarrow \mathbf{2} \text { marks } \\
& =318 & & \\
& =3.2 \times 10^{2} & & \leftarrow \mathbf{1} \text { mark }
\end{array}
$$

b) If the cross-sectional area of the solenoid is $8.5 \times 10^{-4} \mathrm{~m}^{2}$, what is the flux through it?

$$
\begin{aligned}
\Phi & =B A & & \leftarrow \mathbf{1} \text { mark } \\
& =\left(1.2 \times 10^{-2}\right)\left(8.5 \times 10^{-4}\right) & & \leftarrow \mathbf{1} \text { mark } \\
& =1.0 \times 10^{-5} \mathrm{~Wb} & & \leftarrow \mathbf{1} \text { mark }
\end{aligned}
$$

8. The graph shows the light energy $E_{L}$ emitted by a bulb versus time $t$.

a) Find the power output of the bulb.

$$
\begin{array}{rlrl}
P & =\frac{\Delta E}{\Delta t} & \leftarrow \mathbf{1} \mathbf{~ m a r k} \\
& \cong 7.6 \mathrm{~W} & & \leftarrow \mathbf{1} \mathbf{~ m a r k}
\end{array}
$$

b) If this bulb is $20 \%$ efficient, find the power delivered to the bulb.

$$
\begin{aligned}
\frac{P_{\text {out }}}{P_{\text {in }}} & =0.20 \\
\frac{7.6}{P_{\text {in }}} & =0.20 \\
P_{\text {in }} & \cong 38 \mathrm{~W} \quad \leftarrow \mathbf{3} \text { marks }
\end{aligned}
$$

9. In your summer job with the Ministry of Transportation and Highways your supervisor has told you that street signs should no longer be suspended as shown in Diagram A. In order to save money, he would prefer a shorter, perfectly horizontal cable, as shown in Diagram B.


Diagram A


Diagram B

Using principles of physics, argue that the situation in Diagram B is not reasonable.
To balance the weight of the sign there must be an upward force. $\leftarrow \mathbf{2}$ marks
In Diagram $B$ there is no vertical component of the cable tension, and hence no upward force to oppose the weight of the sign. $\leftarrow 2$ marks

