

More Relationships Between Variables - Solutions

1. Consider the equation for the volume of a cylinder

$$V = \pi r^2 h$$

where r represents the radius and h represents the height.

- a) Determine the relationship between volume, V , and radius, r . Express the relationship in both words and symbols. **Volume is directly proportional to the square of radius. $V \propto r^2$**
b) Determine the relationship between volume, V , and height, h . Express the relationship in both words and symbols. **Volume is directly proportional to height. $V \propto h$**

Determine the change in volume for each of the following changes.

- c) The height is increased by a factor of four. **4x**
d) The radius is halved. **1/4x**
e) The radius is decreased by a factor of three and the height is doubled. **2/9x**

A cylindrical glass can hold 400 mL of water. Determine how much water the glass can hold for each of the following changes.

- f) The height is tripled. **1200 mL**
g) The radius is doubled. **1600 mL**
h) The radius is halved and the height is decreased by a factor of four. **25 mL**

2. Consider the equation for magnetic field around a current-carrying wire

$$B = \frac{\mu_0 I}{2\pi d}$$

where μ_0 represents the permeability of free space (a constant), I represents the the current through the wire and d represents distance from the wire.

- a) Determine the relationship between magnetic field, B , and current, I . Express the relationship in both words and symbols.
Magnetic field is directly proportional to current. $B \propto I$
b) Determine the relationship between magnetic field, B , and distance, d . Express the relationship in both words and symbols.
Magnetic field is inversely proportional to distance. $B \propto \frac{1}{d}$

Determine the change in magnetic field for each of the following changes.

- c) The current is halved. **1/2x**
d) The distance from the wire is decreased by a factor of five. **5x**
e) The current is increased by a factor of ten and the distance from the wire is tripled. **10/3x**

A long wire carries a current of 100 mA. At a distance x from the wire, the magnetic field is found to be 20 nT. Determine the magnetic field for each of the following changes.

- f) The current is decreased to 25 mA. **5nT**
g) The distance from the wire is increased to $5x$. **4 nT**
h) The current is increased to 300 mA and the distance from the wire is decreased to $x/4$.
240 nT

3. Consider the equation for the period of a mass-spring oscillator

$$T = 2\pi\sqrt{\frac{m}{k}}$$

where m represents the mass and k represents the spring constant.

- a) Determine the relationship between period, T , and mass, m . Express the relationship in both words and symbols.

Period is directly proportional to the square root of mass. $T \propto \sqrt{m}$

- b) Determine the relationship between period, T , and the spring constant, k . Express the relationship in both words and symbols.

Period is inversely proportional to the square root of the spring constant. $T \propto \frac{1}{\sqrt{k}}$

Determine the change in period for each of the following changes.

- c) The mass is decreased by a factor of four. **1/2x**
d) The spring constant is increased by a factor of nine. **1/3x**
e) The mass and spring constant are both tripled. **no change**

A mass attached to a spring oscillates with a period of 0.80 seconds. Determine the period for each of the following changes.

- f) The spring constant is decreased by a factor of four. **1.6 s**
g) The mass is increased by a factor of 25. **4.0 s**
h) The mass is halved and the spring constant is increased by a factor of eight. **0.20 s**

4. Consider the equation for the electric force between two charges

$$F_e = k \frac{q_1 q_2}{r^2}$$

where k represents the electrostatic constant, q_1 and q_2 represent the charges and r represents the separation distance.

Two charges are separated by a distance of 20 mm. The electric force at this distance is 2 N. Determine the electric force between the charges for the following changes.

- a) One charge is halved. **1 N**
b) Both charges are increased by a factor of three. **18 N**
c) The distance separating the charges is increased to 100 mm. **0.08 N**
d) The distance separating the charges is decreased to 10 mm. **8 N**
e) The distance separating the charges is decreased to 50 mm. **0.32 N**
f) One charge is halved and the distance separating the charges is decreased to 10 mm. **4 N**
g) Both charges are increased by a factor of ten and the distance separating the masses is increased to 100 mm. **8 N**
h) One charge is doubled, the other is decreased by a factor of five, and the distance separating them is decreased to 4 mm. **20 N**