

CONSERVATION OF ENERGY - SOLUTIONS

1. GIVEN:

$$m = 1.0 \text{ kg}$$

$$h_i = 90 \text{ m}$$

$$h_f = 70 \text{ m}$$

$$E_{k_i} = 0$$

$$E_{k_f} = ?$$

$$E_i = E_f$$

$$E_{k_i} + E_{p_i} = E_{k_f} + E_{p_f}$$

$$E_{k_i} + mgh_i = E_{k_f} + mgh_f$$

$$E_{k_f} = mgh_i - mgh_f$$

$$= mg(h_i - h_f)$$

$$= (1.0)(9.8)(90 - 70)$$

$$= 196 \text{ J}$$

$$200 \text{ J}$$

2. GIVEN:

$$m = 0.50 \text{ kg}$$

$$E_{k_i} = 25 \text{ J}$$

$$E_{k_f} = 0$$

$$h_i = 0$$

$$h_f = ?$$

$v = 0$ at highest
Point $\rightarrow E_k = 0$

$$E_i = E_f$$

$$E_{k_i} + E_{p_i} = E_{k_f} + E_{p_f}$$

$$E_{k_i} + mgh_i = E_{k_f} + mgh_f$$

$$E_{k_i} = mgh_f$$

$$h_f = \frac{E_{k_i}}{mg}$$

$$= \frac{25}{(0.50)(9.8)}$$

$$= 5.1 \text{ m}$$

3. GIVEN:
 $m = 1.00 \text{ kg}$
 $v_i = 0$
 $v_f = 12.0 \frac{\text{m}}{\text{s}}$
 $E_{p_i} = ?$
 $E_{p_f} = 0$

$$E_i = E_f$$

$$E_{k_i} + E_{p_i} = E_{k_f} + E_{p_f}$$

$$\cancel{\frac{1}{2}mv_i^2} + E_{p_i} = \frac{1}{2}mv_f^2 + \cancel{E_{p_f}}$$

$$E_{p_i} = \frac{1}{2}mv_f^2$$

$$= \frac{1}{2}(1.00)(12.0)^2$$

$$= 72.0 \text{ J}$$

4. a) GIVEN:
 $m = 3.0 \text{ kg}$
 $h = 3.0 \text{ m}$

$$E_p = mgh$$

$$= (3.0)(9.8)(3.0)$$

$$= 88 \text{ J}$$

b) GIVEN:
 $m = 3.0 \text{ kg}$
 $v_i = 0$
 $v_f = ?$
 $h_i = 3.0 \text{ m}$
 $h_f = 1.0 \text{ m}$

$$E_i = E_f$$

$$E_{k_i} + E_{p_i} = E_{k_f} + E_{p_f}$$

$$\cancel{\frac{1}{2}mv_i^2} + mgh_i = \frac{1}{2}mv_f^2 + mgh_f$$

$$\cancel{mgh_i} = \frac{1}{2}\cancel{mv_f^2} + \cancel{mgh_f}$$

$$\frac{1}{2}v_f^2 = gh_i - gh_f$$

$$v_f = \sqrt{2g(h_i - h_f)}$$

$$= \sqrt{2(9.8)(3.00 - 1.00)}$$

$$= 6.3 \frac{\text{m}}{\text{s}}$$

c)

GIVEN:

$$m = 3.0 \text{ kg}$$

$$v_i = 0$$

$$v_f = ?$$

$$h_i = 3.0 \text{ m}$$

$$h_f = 0$$

$$E_i = E_f$$

$$E_{k_i} + E_{p_i} = E_{k_f} + E_{p_f}$$

$$\frac{1}{2}mv_i^2 + mgh_i = \frac{1}{2}mv_f^2 + mgh_f$$

$$mgh_i = \frac{1}{2}mv_f^2$$

$$gh_i = \frac{1}{2}v_f^2$$

$$v_f = \sqrt{2gh_i}$$

$$= \sqrt{2(9.8)(3.00)}$$

$$= 7.7 \frac{\text{m}}{\text{s}}$$

d)

G : AT THAT POINT, ALL THE ENERGY IS POTENTIAL (SAME HEIGHT AS A).

5.

GIVEN:

$$m = 85.0 \text{ kg}$$

$$v_i = 6.00 \frac{\text{m}}{\text{s}}$$

$$v_f = 0$$

$$h_i = 0$$

$$h_f = ?$$

$$E_i = E_f$$

$$E_{k_i} + E_{p_i} = E_{k_f} + E_{p_f}$$

$$\frac{1}{2}mv_i^2 + mgh_i = \frac{1}{2}mv_f^2 + mgh_f$$

$$\frac{1}{2}mv_i^2 = mgh_f$$

$$\frac{1}{2}v_i^2 = gh_f$$

$$h_f = \frac{v_i^2}{2g}$$

$$= \frac{(6.00)^2}{2(9.8)}$$

$$= 1.8 \text{ m}$$

6. a) GIVEN:

$$m = 500. \text{ kg}$$

$$v_i = 1.2 \frac{\text{m}}{\text{s}}$$

$$v_f = ?$$

$$h_i = 30.0 \text{ m}$$

$$h_f = 25.0 \text{ m}$$

$$E_i = E_f$$

$$E_{k,i} + E_{p,i} = E_{k,f} + E_{p,f}$$

$$\frac{1}{2} m v_i^2 + m g h_i = \frac{1}{2} m v_f^2 + m g h_f$$

$$\frac{1}{2} v_i^2 + g h_i = \frac{1}{2} v_f^2 + g h_f$$

$$\frac{1}{2} v_f^2 = \frac{1}{2} v_i^2 + g h_i - g h_f$$

$$v_f = \sqrt{2 \left(\frac{1}{2} v_i^2 + g h_i - g h_f \right)}$$

$$= \sqrt{2 \left[\frac{1}{2} (1.20)^2 + (9.8)(30.0) - (9.8)(25.0) \right]}$$

$$= 10. \frac{\text{m}}{\text{s}}$$

b) GIVEN:

$$m = 500. \text{ kg}$$

$$v_i = 1.2 \frac{\text{m}}{\text{s}}$$

$$v_f = ?$$

$$h_i = 30.0 \text{ m}$$

$$h_f = 12.0 \text{ m}$$

$$E_i = E_f$$

$$E_{k,i} + E_{p,i} = E_{k,f} + E_{p,f}$$

$$\frac{1}{2} m v_i^2 + m g h_i = \frac{1}{2} m v_f^2 + m g h_f$$

$$\frac{1}{2} v_i^2 + g h_i = \frac{1}{2} v_f^2 + g h_f$$

$$\frac{1}{2} v_f^2 = \frac{1}{2} v_i^2 + g h_i - g h_f$$

$$v_f = \sqrt{2 \left(\frac{1}{2} v_i^2 + g h_i - g h_f \right)}$$

$$= \sqrt{2 \left[\frac{1}{2} (1.20)^2 + (9.8)(30.0) - (9.8)(12.0) \right]}$$

$$= 19 \frac{\text{m}}{\text{s}}$$

c) GIVEN:

$$m = 500. \text{ kg}$$

$$v_i = 1.2 \frac{\text{m}}{\text{s}}$$

$$v_f = ?$$

$$h_i = 30.0 \text{ m}$$

$$h_f = 0$$

$$E_i = E_f$$

$$E_{k_i} + E_{p_i} = E_{k_f} + E_{p_f} \quad h_f = 0$$

$$\frac{1}{2}mv_i^2 + mgh_i = \frac{1}{2}mv_f^2 + mgh_f$$

$$\frac{1}{2}mv_i^2 + mgh_i = \frac{1}{2}mv_f^2$$

$$\frac{1}{2}v_i^2 + gh_i = \frac{1}{2}v_f^2$$

$$v_f = \sqrt{2\left(\frac{1}{2}v_i^2 + gh_i\right)}$$
$$= \sqrt{2\left[\frac{1}{2}(1.2)^2 + (9.8)(30.0)\right]}$$

$$= 24 \frac{\text{m}}{\text{s}}$$

7. GIVEN:

$$v_i = ?$$

$$v_f = 0$$

$$h_i = 0$$

$$h_f = 5.20 \text{ m}$$

$$E_i = E_f$$

$$E_{k_i} + E_{p_i} = E_{k_f} + E_{p_f} \quad h_i = 0 \quad v_f = 0$$

$$\frac{1}{2}mv_i^2 + mgh_i = \frac{1}{2}mv_f^2 + mgh_f$$

$$\frac{1}{2}mv_i^2 = mgh_f$$

$$\frac{1}{2}v_i^2 = gh_f$$

$$v_i = \sqrt{2gh_f}$$

$$= \sqrt{2(9.8)(5.20)}$$

$$= 10. \frac{\text{m}}{\text{s}}$$

8. GIVEN:
 $m = 65 \text{ kg}$
 $v_i = ?$
 $v_f = 0$
 $h_i = 0$
 $h_f = 5.5 \text{ m}$

$$E_i = E_f$$

$$E_{k_i} + E_{p_i} = E_{k_f} + E_{p_f}$$

$$\frac{1}{2}mv_i^2 + mgh_i = \frac{1}{2}mv_f^2 + mgh_f$$

$$\frac{1}{2}mv_i^2 = mgh_f$$

$$v_i = \sqrt{2gh_f}$$

$$= \sqrt{2(9.8)(5.5)}$$

$$= 10.38 \text{ m}$$

$$10. \text{ m}$$

9. GIVEN:
 $m = 55 \text{ kg}$
 $v_i = 0$
 $h_i = 3.00 \text{ m}$
 $h_f = 1.00 \text{ m}$
 $E_{p_i} = ?$
 $E_{k_f} = ?$

$$E_{p_f} = mgh_f$$

$$= (55)(9.8)(1.00)$$

$$= 539 \text{ J}$$

$$540 \text{ J}$$

$$E_i = E_f$$

$$E_{k_i} + E_{p_i} = E_{k_f} + E_{p_f}$$

$$\frac{1}{2}mv_i^2 + mgh_i = E_{k_f} + mgh_f$$

$$E_{k_f} = mgh_i - mgh_f$$

$$= mg(h_i - h_f)$$

$$= (55)(9.8)(3.00 - 1.00)$$

$$= 1078 \text{ J}$$

$$1100 \text{ J}$$

10.

GIVEN:

$$v_i = 0$$

$$v_f = 7.0 \frac{m}{s}$$

$$h_i = ?$$

$$h_f = 0$$

$$E_i = E_f$$

$$E_{ki} + E_{pi} = E_{kf} + E_{pf}$$

$$\cancel{\frac{1}{2}mv_i^2} + mgh_i = \cancel{\frac{1}{2}mv_f^2} + mgh_f$$

$$mgh_i = \cancel{\frac{1}{2}mv_f^2}$$

$$h_i = \frac{v_f^2}{2g}$$

$$= \frac{(7.0)^2}{2(9.8)}$$

$$= 2.5 m$$

11.

GIVEN:

$$m = 7.50 \text{ kg}$$

$$v_i = 0$$

$$v_f = ?$$

$$h_i = 1.5 m$$

$$h_f = 0$$

$$E_i = E_f$$

$$E_{ki} + E_{pi} = E_{kf} + E_{pf}$$

$$\cancel{\frac{1}{2}mv_i^2} + mgh_i = \cancel{\frac{1}{2}mv_f^2} + mgh_f$$

$$mgh_i = \cancel{\frac{1}{2}mv_f^2}$$

$$v_f = \sqrt{2gh_i}$$

$$= \sqrt{2(9.8)(1.5)}$$

$$= 5.4 \frac{m}{s}$$

12.

GIVEN:

$$v_i = 6.0 \frac{\text{m}}{\text{s}}$$

$$v_f = 0$$

$$h_i = 2.0 \text{ m}$$

$$h_f = ?$$

ONE WAY TO SOLVE THIS PROBLEM IS TO FIND THE MAXIMUM HEIGHT SHE CAN REACH (SET $v_f = 0$ AND SOLVE FOR h_f). IF $h_f \geq 4.0 \text{ m}$, SHE MAKES IT TO THE TOP OF THE HILL.

$$E_i = E_f$$

$$E_{k_i} + E_{p_i} = E_{k_f} + E_{p_f}$$

$$\frac{1}{2}mv_i^2 + mgh_i = \frac{1}{2}mv_f^2 + mgh_f$$

$$\cancel{\frac{1}{2}mv_i^2} + \cancel{mgh_i} = \cancel{mgh_f}$$

$$h_f = \frac{\frac{1}{2}v_i^2 + gh_i}{g}$$

$$= \frac{\frac{1}{2}(6.0)^2 + (9.8)(2.0)}{(9.8)}$$

$$= 3.8 \text{ m}$$

NO, SHE WILL NOT MAKE IT UP THE 4.0 m HILL.

13. GIVEN:

$$m = m$$

$$v_i = 0$$

$$v_f = ?$$

$$h_i = h$$

$$h_f = 0$$

$$E_i = E_f$$

$$E_{ki} + E_{pi} = E_{kf} + E_{pf}$$

$$\cancel{\frac{1}{2}mv_i^2} + mgh_i = \cancel{\frac{1}{2}mv_f^2} + \cancel{mgh_f}$$

$$\cancel{mgh_i} = \cancel{\frac{1}{2}mv_f^2}$$

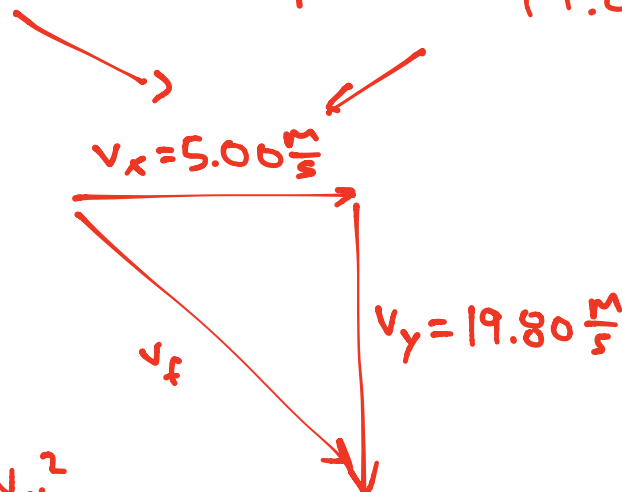
$$v_f = \sqrt{2gh_i}$$

$$= \sqrt{2(9.8)h}$$

$$= \sqrt{19.6h}$$

14. a)

x	y
$v = 5.0 \frac{m}{s}$	$v_i = 0$
	$v_f = ?$
	$d = 20.0 \text{ m}$
	$a = 9.8 \frac{m}{s^2}$
	$v_f^2 = v_i^2 + 2ad$
	$v_f = \sqrt{2ad}$
	$= \sqrt{2(9.8)(20.0)}$
	$= 19.80 \frac{m}{s}$



$$\begin{aligned} v_f^2 &= v_x^2 + v_y^2 \\ v_f &= \sqrt{v_x^2 + v_y^2} \\ &= \sqrt{(5.00)^2 + (19.80)^2} \\ &= 20. \frac{m}{s} \end{aligned}$$

b) GIVEN:

$$v_i = 5.00 \frac{m}{s}$$

$$v_f = ?$$

$$h_i = 20.0 m$$

$$h_f = 0$$

$$E_i = E_f$$

$$E_{K_i} + E_{P_i} = E_{K_f} + E_{P_f} \quad h_f = 0$$

$$\frac{1}{2}mv_i^2 + mgh_i = \frac{1}{2}mv_f^2 + mgh_f$$

$$\frac{1}{2}mv_i^2 + mgh_i = \frac{1}{2}mv_f^2$$

$$\frac{1}{2}v_i^2 + gh_i = \frac{1}{2}v_f^2$$

$$v_f = \sqrt{2\left(\frac{1}{2}v_i^2 + gh_i\right)}$$

$$= \sqrt{2\left[\frac{1}{2}(5.00)^2 + (9.8)(20.0)\right]}$$

$$= 20. \frac{m}{s}$$